The improvement of an elastic hinge-type torque standard machine in NIMT

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ABSTRACT
The National Institute of Metrology of Thailand’s (NIMT) strain-controlled elastic hinge-type torque standard machine was designed to cover a measuring range of 1 N·m to 1 kN·m. The elastic hinge was used both at the fulcrum and the hanger of lever arms. The designed elastic hinge’s thickness, 0.50 mm, caused a higher stiffness than a sheet metal plate of other types of torque machines. The bending moment of all elastic hinges affected the sum of the torque signal on the lever arm that was used to observe the balancing of the lever. The residual torque sensitivity, which was no better than 0.20 mN·m, significantly affected the uncertainty of the low-range torque realisation.

The calibration and measurement capabilities of the machine were 0.010 % (k = 2) in the measurement range of 10 N·m to 1 kN·m and 0.030 % (k = 2) in the measurement range of 1 N·m to 10 N·m. In the transducer calibration, the influence of the random bending moment of the elastic hinge affected the repeatability, reproducibility, and linearity of the low torque measurements. The cause of the bending moment of the elastic hinges was a result of the deviation of the centre of gravity (CG) of the weight on the pan from the reference line. To improve CMCs, separate signal calibrations were selected for this experiment i.e. the left hinge, the right hinge, and the fulcrum. The torque in each signal calibration was combined by software and was used to correct the calibration value of the torque.

1. INTRODUCTION

NIMT’s 1 kN·m elastic hinge-type torque standard machine (TSM) [1,2,3,4] was established in 2004. The machine was designed and assembled by GTM GmbH in Germany. Unfortunately, the left elastic hinge was damaged during the commissioning process at NIMT’s Bangkok site. In 2005, the NIMT moved it to a new site in Pathumthani. The machine was reconstructed, including the replacement of the damaged parts and recalibration. The calibration and measurement capabilities (CMCs) were 0.010 % (k = 2) in the measurement range of 10 N·m to 1 kN·m and 0.030 % (k = 2) in the measurement range of 1 N·m to 10 N·m. The CMCs were proven by the CCMT-K1.2 comparison in 2008 [5]. The final report was published in 2015.

In 2013, it was found that the machine had problems caused by the residual torque signal from the fulcrum cross-elastic hinge. The problem was resolved by using the displacement sensor to detect the balance position of the lever instead of the damaged elastic hinge. In 2014, the mechanical fulcrum cross-elastic hinge completely malfunctioned due to the deformation of its plastic, and this must be replaced. The new fulcrum cross-elastic hinge was procured from the manufacturer and was replaced by NIMT staff in the same year. The CMCs were confirmed again by some bilateral comparisons (compared with a PTB certificate and the 10 N·m TSM of NIMT [6,7,8]). This was our chance to study the strain-controlled elastic hinge characteristic based on each repair and maintenance exercise. The most important point of the machine's realisation was a residual torque that was a dominant uncertainty contribution. NIMT was interested in determining the method of reducing the uncertainty of measurement caused by the residual torque signal.
2. RESIDUAL TORQUE CONFIGURATION

The original residual torque signal was configured by the manufacturer. The output residual torque signal combined four signals (left hinge, channel 1; right hinge, channel 2; and fulcrum front and rear, channels 3 and 4) by using the electric circuit. The sensitivity of the signals of the left and right hinges was reduced tenfold by using normal resistors with the same resistance on both sides. The reduced signals and the fulcrum signals were combined. The manufacturer aimed to reduce the influence of the left and right elastic hinge signals that would affect the combined signals.

The combined signals were converted to a torque unit by an Analogic AN3060 digital weight indicator [9], as shown in Figure 1.

The original residual torque configuration should be realized by the separate signal calibrations as performed in this experiment: left hinge, right hinge, and fulcrum. The residual torque in each signal calibration was combined by software and was used to correct the calibration torque value.

3. BENDING MOMENT OF ELASTIC HINGE

3.1. Asymmetric load

The imperfection of the manufacturing process of the weight set caused an asymmetric load distribution. Additionally, small steel balls were used to adjust the mass of the weight set. The weight stack on the pan touched the column, and many steel balls inside changed the position independently, as shown in Figure 2. Both of these cases might cause the bending moment at the elastic hinge of lever arm.

\[ \sum M = 0 \]  
\[ M_T - F_1 \cdot L_1 - M_B = 0 \]  

The hypothesis of the asymmetric load was proven by the finite element analysis (FEA) at NIMT. Static analysis was selected for studying the stress, the displacement, and the strain of the elastic hinges. The FEA simulation was designed by applying the 0.5 N forces on the centre position, at 60 mm from the centre and 120 mm from the centre. The elastic hinge geometry was divided into a finite element by a curvature-based mesh algorithm. These small meshes were controlled in the areas in which there is a rapid change in stress, while the large meshes were controlled in the areas in which there was little change in stress [10]. Obviously, the bending value of the elastic hinge depends on the distance of the force on the pan, as shown in Figure 3.

3.2. The moment of force

As evident in Figure 4, the centre of the gravitational force acting on the hinge shifted from the original position due to the stacked weights. In this case, the bending moment, \( M_B \), was not equal to zero. That variable was effected by the calibration torque, \( M_T \), as in Equation (2). The measured bending moment of the elastic hinge should be considered:

\[ \sum M = 0 \]  
\[ M_T - F_1 \cdot L_1 - M_B = 0 \]  

Figure 2. Asymmetric load on the pan due to the imperfection of the manufacturing and the steel balls inside.
The fulcrum was preloaded three times at approximately 5 mN·m. Then, the weight was applied onto the reference position (as shown in Figure 6), as the calibration steps are shown in Figure 7, three times. The weight steps were 50 mg, 100 mg, 200 mg, and 500 mg, respectively. The measurement process was done using the left and right pans. In the meantime, the data channel was recorded. Together, the strain signals of clockwise and anticlockwise torque were expressed as a function of the torque by the first-order linear interpolation equation, without the absolute term.

\[ M_B = M_T - F_1 \cdot L_4 \]  

(3)

where:

- \( F_1 \) is the force,
- \( L_4 \) is the lever length (approx. 500 mm).

4. EXPERIMENT

The measured moment of the strain-controlled elastic hinges is realised by considering the signal separation. The indicating device was changed to a four-channel HBM MGCplus synchronous amplifier (1×ML38 and 3×ML30B) [11]. The signal was separated from the combined circuit box: Ch1; right hinge, Ch2; left hinge and Ch3+Ch4; fulcrum front and rear. The Ch1, Ch2, Ch3+Ch4, and the transducer were connected to the amplifier, as shown in Figure 5. The transducer did not connect to the TSM. Next, we performed the activities as described in sections 4.1 to 4.4.

4.1. Fulcrum cross-elastic hinge realisation

The fulcrum was preloaded three times at approximately 5 mN·m. We recorded the data channel. Together, the strain signals of clockwise and anticlockwise torque were expressed as a function of the torque by the first-order linear interpolation equation, without the absolute term.

4.2. Left and right elastic hinges realisation

A recognised torque transducer (Rauter; TT1/10 N·m) [12] was used to transfer the torque value to both sides of the elastic hinges. The TT1/10 N·m was calibrated by the 10 N·m TSM of NIMT [6,7] in the measurement range of 0.1 N·m to 1 N·m. The repeatability and linearity of the measurement results of TT1/10 N·m at 0.2 N·m were within 0.002 % and 0.004 %, respectively. The measurements should be carried out separately for the right and left torques. The next steps were to connect the transducer to the machine, as shown in Figure 8, preload three times at approximately 0.25 N·m (50 g weight), and wait for three minutes. Then, we recorded the data channel. The weight steps were 50 mg, 100 mg, 200 mg, and 500 mg, respectively. The measurements should be carried out separately for the right and left torques. The next steps were to connect the transducer to the machine, as shown in Figure 8, preload three times at approximately 0.25 N·m (50 g weight), and wait for three minutes. Then, we recorded the data channel. The measurement results of TT1/10 N·m at 0.2 N·m were within 0.002 % and 0.004 %, respectively. The measurements should be carried out separately for the right and left torques. The next steps were to connect the transducer to the machine, as shown in Figure 8, preload three times at approximately 0.25 N·m (50 g weight), and wait for three minutes. Then, we recorded the data channel. The measurement results of TT1/10 N·m at 0.2 N·m were within 0.002 % and 0.004 %, respectively. The measurements should be carried out separately for the right and left torques. The next steps were to connect the transducer to the machine, as shown in Figure 8, preload three times at approximately 0.25 N·m (50 g weight), and wait for three minutes. Then, we recorded the data channel.
Figure 9. Difference in arm length between the left and right arms.

Figure 9. The measurement in each range must be done for three cycles. If the system is in equilibrium, the clockwise torques, $M_1$ and anti-clockwise torque, $M_2$ shall be equal. The difference in arm length, $l_D$, was calculated by Equations (4) to (9).

\[
M_1 = M_2 \tag{4}
\]

\[
F_1 \cdot (L - l_D) = F_2 \cdot (L + l_D) \tag{5}
\]

\[
F_1 \cdot L - F_1 \cdot l_D = F_2 \cdot L + F_2 \cdot l_D \tag{6}
\]

\[
F_1 \cdot L - F_2 \cdot L = l_D \cdot (F_1 + F_2) \tag{7}
\]

\[
l_D = \frac{(F_2 \cdot L - F_1 \cdot L)}{(F_1 + F_2)} \tag{8}
\]

4.4. Torque transducer calibration

The realised residual torque from Ch1, Ch2, and Ch3+Ch4 was combined by a software program (shown in Figure 10) used to monitor and correct the calibration torque value in the calibration process. The proposed method was proven reliable by comparing the transducer calibration results characteristics: the repeatability, reproducibility, and linearity of the measurement according to the German Industrial Standard documentation DIN 51309 [14].

5. EXPERIMENTAL RESULTS

5.1. Fulcrum cross-elastic hinge realisation results

Two cross elastic hinges’ signals at the fulcrum (Ch3+Ch4) were expressed as a function of torque by using the first order of the interpolation equation without the absolute term, as shown in Figure 11. The interpolation deviation results were within ± 0.0002 N-m, as shown in Figure 12. That was a limitation of the fulcrum sensitivity of the machine, which was due to the designed elastic hinge’s thickness, 0.50 mm, causing a higher stiffness compared to the sheet metal plate of the other types of TSMs.

5.2. Left and right elastic hinges realisation results

The calibration results for the bending moment of the elastic hinge are shown in Table 1 and Table 2. It is clear that the torque calibration in which the weight was not put on the pan did not change. That meant the moment of the hinge was zero. The weight placed at each position on the pan from the reference line in any direction caused a varied torque vector, as shown in Figure 13. It was therefore possible to determine the sensitivity, as shown in Figure 14. It was found that the sensitivities of the left and right elastic hinges were different.
The residual torque of the machine, $M_R$, was calculated by a summation of the torque vector signals at the fulcrum (Ch3+Ch4), a bending moment of the right elastic hinge (Ch1), and a bending moment of the left (Ch2). The calibration torque, $M_{C1}$, was calculated by a summation of the torque vectors, including the generated torque ($F_1 \cdot L_1$) and the residual torque value $M_R$.

### 5.3. Difference in arm length evaluation results

The difference in the arm length between the left and right arms varied between 23 µm and 33 µm, as shown in Figure 15. The difference in the lever arm length in each couple force step was expressed as a function of length by a third order interpolation equation, including the absolute term. The difference in arm length must be used to correct the effective lever arm length, $L_i$, for each calibration torque value. The shift in the difference of arm length had a direct effect on the linearity of the calibration. The difference in the arm length, $\Delta l_i$ (in micrometres), of each calibration torque step, $M_{C1}$, was calculated by Equation (10).

$$
\Delta l_i = -0.000007 M_i^2 + 0.0002 M_i^2 - 0.0773 M_i + 32.593
$$

The influence of the variation in the difference in arm length (10 µm) affected the linearity of the measurement by about 2 ppm relative to the lever arm of 500 mm and affected the certified output signals of the transducer under calibration by about 7 ppm. However, the difference in arm length of each calibration torque step was used to calculate the effective lever arm length, $L_i$, by summing it with half of the entire measured lever length. The uncertainty in the different length evaluation and entire lever length measurement must be taken into account.

### 5.4. The comparison results of the torque transducer calibration characteristics

The calibration torque, $M_{C1}$, was corrected by the residual torque value and the difference in arm length of both configurations (original and this research’s concepts). However, the original configuration of the residual torque did not concern the bending moment from the asymmetrical load. The measurement results for the torque transducer calibration were interpolated to the nominal torque value. The comparison results for the repeatability, reproducibility, and linearity characteristics are shown in Figure 16, Figure 17 and Figure 18, respectively. Those results were a calibration of the same transducer, but different configurations for the residual torque signal. The random bending moment affected the repeatability, reproducibility, and linearity of measurement.

It was found from the experiment that the residual torque combined with the bending moment could be used to correct the calibration torque value, because the actual residual torque sensitivity was calibrated. Considering the above three parameters, this research proposed a method of significantly improving the torque calibration’s characteristics.

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**Table 2. Ch2; Anti-clockwise torque measurement results.**

<table>
<thead>
<tr>
<th>Mass position in m</th>
<th>Transducer in N·m</th>
<th>Ch3+Ch4 in N·m</th>
<th>Output signal in mV/V</th>
</tr>
</thead>
<tbody>
<tr>
<td>P_4</td>
<td>-0.12</td>
<td>-0.24009</td>
<td>-0.00001</td>
</tr>
<tr>
<td>P_3</td>
<td>-0.09</td>
<td>-0.24257</td>
<td>0.00002</td>
</tr>
<tr>
<td>P_2</td>
<td>-0.06</td>
<td>-0.24504</td>
<td>0.00006</td>
</tr>
<tr>
<td>P_1</td>
<td>-0.03</td>
<td>-0.24750</td>
<td>0.00004</td>
</tr>
<tr>
<td>Ref.</td>
<td>0</td>
<td>-0.24995</td>
<td>0.00003</td>
</tr>
<tr>
<td>P_1</td>
<td>0.03</td>
<td>-0.25233</td>
<td>0.00000</td>
</tr>
<tr>
<td>P_2</td>
<td>0.06</td>
<td>-0.25470</td>
<td>-0.00002</td>
</tr>
<tr>
<td>P_3</td>
<td>0.09</td>
<td>-0.25721</td>
<td>0.00001</td>
</tr>
<tr>
<td>P_4</td>
<td>0.12</td>
<td>-0.25973</td>
<td>0.00003</td>
</tr>
</tbody>
</table>

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**Figure 13. Varied torque by mass position.**

**Figure 14. Linear regression of the Ch1 and Ch2 signals.**

**Figure 15. Change in the difference in arm length.**

**Figure 16. The repeatability characteristic.**
6. CONCLUSIONS

The bending moments of the right and left elastic hinges were the results of the force-applied position that deviated from the reference line. The cause of the misposition of the applied force was a result of an imperfection in the manufacturer’s process and a small steel ball inside the weight.

The proposed method in this research can resolve the undesirable influence of the bending moment of elastic hinges by significantly improving the repeatability, reproducibility, and linearity of the measurement. In the future, the problem with the asymmetric load should be corrected by the fabrication of new standard weights.

The holder of the strain controlled elastic hinge type torque standard machine should be considered the influence of the bending moment, which affected the uncertainty of the measurement in a low torque calibration, especially when it was lower than 1.0 % of the maximum capacity of the machine.

The calibration and measurement capabilities (CMCs) was still maintained at 0.030 % (k = 2) at the measurement range 1 N·m to 10 N·m. However, the CMCs at the measurement range 2 N·m to 10 N·m was improved to 0.020 % (k = 2).

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